

# learning focus:

- ✓ differentiate between multiplicative and additive relationships
- ✓ identify independent and dependent quantities from tables and graphs
- ✓ represent situations using verbal descriptions, tables, graphs, and equations

## ALGEBRAIC REPRESENTATIONS UNIT

### 8 DAY TEKS-ALIGNED UNIT



#### ALGEBRAIC REPRESENTATIONS UNIT

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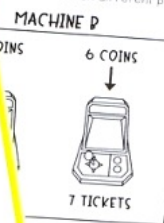
#### ALGEBRAIC REPRESENTATIONS

##### PACING GUIDE

games to play. Each game requires a ticket in for prizes before leaving the

two machines below. They determine tickets based on different patterns.

**TASK 1:**



# ALGEBRAIC REPRESENTATIONS



an 8 day TEKS-aligned unit

TEKS: 6.4A, 6.6A, 6.6B, 6.6C, 6.11A

**ready-to-go, scaffolded  
student materials**

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# ALGEBRAIC REPRESENTATIONS



an 8 day TEKS-aligned unit

TEKS: 6.4A, 6.6A, 6.6B, 6.6C, 6.11A

## student friendly + real-world application

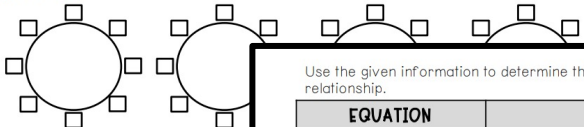
multiple representations

Unit: Algebraic Representations  
Student Handout 2

Name \_\_\_\_\_  
Date \_\_\_\_\_ Pd \_\_\_\_\_

### MULTIPLICATIVE RELATIONSHIPS

An event planner is organizing the seating chart at a wedding reception. She has drawn the diagram below.



a. Describe the ratio of tables to chairs.  
b. If the wedding now needed six tables,

A multiplicative relationship is shown by the equation  $y = ax$ .

- $y = 7x$
- $x = 7y$
- $a = 7$
- The  $a$ -value is the multiplier in a multiplicative relationship.

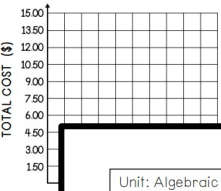
### MULTIPLICATIVE RELATIONSHIPS

In the tables below, complete the process equation in the form  $y = ax$ .

| X | PROCESS | Y  |
|---|---------|----|
| 2 |         | 8  |
| 3 |         | 12 |
| 4 |         | 16 |
| 5 |         | 20 |
| 6 |         | 24 |

A = \_\_\_\_\_ EQUATION = \_\_\_\_\_

Use the given information to determine the missing representations for each multiplicative relationship.

| EQUATION                                 | GRAPH  | TABLE |
|--|--|-------|
|  |  |       |
| DESCRIPTION                              |  |       |
| The cost of an ice cream cone is \$1.50. |  |       |

Summarize today's lesson:

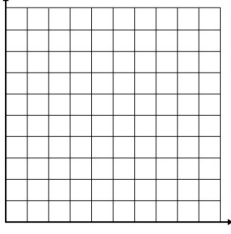
Unit: Algebraic Representations  
Homework 2

Name \_\_\_\_\_  
Date \_\_\_\_\_ Pd \_\_\_\_\_

### MULTIPLICATIVE RELATIONSHIPS


Use your understanding of multiplicative relationships to answer the questions below.

- The Suarez family travels 70 miles per hour on their family road trip. Represent the number of miles traveled with  $m$ , and time with  $t$ .
  - Complete the table below.

| T |  |  |  |  |
|---|--|--|--|--|
| M |  |  |  |  |
  - Write an equation to describe the situation.
  - Graph the situation below.
- The table shows the relationship between the number of hours worked and the total earnings. Which equation best represents the relationship in the table?

| # OF HOURS (H)     | 1  | 2  | 3  | 4  | 5  |
|--------------------|----|----|----|----|----|
| TOTAL EARNINGS (T) | 12 | 24 | 36 | 48 | 60 |

  - $h = 12t$
  - $t = 12h$
  - $h = \frac{c}{12}$
  - $c = \frac{h}{12}$
- The movie theater sells a bucket of popcorn,  $p$ , for \$5.95 each. Which of the following equations best represents  $c$ , the total cost of purchasing buckets of popcorn?
  - $c = 5.95p$
  - $p = 5.96c$
  - $c + 5.95 = p$
  - $p + c = 5.95$



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graphic organizers

# ALGEBRAIC REPRESENTATIONS



an 8 day TEKS-aligned unit

TEKS: 6.4A, 6.6A, 6.6B, 6.6C, 6.11A

streamline your planning  
process with unit overviews

## ALGEBRAIC REPRESENTATIONS OVERVIEW



### READINESS STANDARDS

**6.6C** Represent a given situation using verbal descriptions, tables, graphs, and equations in the form  $y = kx$  or  $y = x + b$ .

**6.11A** Graph points in all four quadrants using ordered pairs of rational numbers. *(More formally included in Unit 9 Geometry)*

### SUPPORTING STANDARDS

**6.4A** Compare two rules verbally, numerically, graphically, and symbolically in the form of  $y = ax$  or  $y = x + a$  in order to differentiate between additive and multiplicative relationships.

**6.6A** Identify independent and dependent quantities from tables and graphs.

**6.6B** Write an equation that represents the relationship between independent and dependent quantities from a table.



key vocabulary



vertical alignment



sample  
pacing  
calendar

### PIC IDEAS

- Mathematical relationships: descriptions.
- Additive relationships do not through the origin.

### ESSENTIAL QUESTION

- How can a situation be represented?
- What differences are there?

## ALGEBRAIC REPRESENTATIONS PACING GUIDE



| DAY 1                               | DAY 2                                      | DAY 3                  | DAY 4                                     | DAY 5                          |
|-------------------------------------|--|------------------------|---|--------------------------------|
| Review of Graphing and Tables       | Multiplicative Relationships               | Additive Relationships | Multiplicative vs. Additive Relationships | Algebraic Representations Quiz |
| Student Handout 1 Homework 1        | Student Handout 2 Homework 2               |                        |   |                                |
| DAY 6                               | DAY 7                                      | DAY 8                  | DAY 9                                     | DAY 10                         |
| Independent and Dependent Variables | Algebraic Representations Unit Study Guide |                        |   |                                |
| Student Handout 5 Homework 5        | Unit Study Guide                           |                        |   |                                |

## ALGEBRAIC REPRESENTATIONS OVERVIEW



| TOPIC                               | TEACHING TIPS   |
|-------------------------------------|---|
| Review of Graphing and Tables       | <ul style="list-style-type: none"> <li>Using masking tape or painter's tape, create a life-sized coordinate plane and have students practice finding ordered pairs and giving directions to each other. Online, I have seen this idea created on a white shower curtain so it can be moved. For a more technologically-friendly idea, consider projecting the coordinate plane and using magnets.</li> <li>If you feel confident that your students are successful with this concept, then you could have them plot a picture on a page, get with a partner, and swap directions.</li> </ul>  |
| Multiplicative Relationships        | <ul style="list-style-type: none"> <li>For some reason, multiplicative relationships are slightly more intuitive to students. I really like asking students to create the process column when working with tables, so they can see the consistency in "a," when <math>y = ax</math>.</li> <li>Project four different languages all saying the word "hello." You could even use a translator app to have the word read aloud. Then, help students to understand that the words all mean the same thing. The biggest takeaway here is to ensure that students understand that each of these relationships (verbal, equation, graph, table) can be represented in different ways.</li> </ul> |
| Additive Relationships              | <ul style="list-style-type: none"> <li>Additive relationships can be more confusing because they do not go through the origin and thus do not have the ordered pair <math>(0, 0)</math>. Students must be able to find out what the y-value is when x is zero. This value will represent "a" when <math>y = x + a</math>.</li> </ul>  |
| Independent and Dependent Variables | <ul style="list-style-type: none"> <li>In science class, many teachers use the acronym DRY MIX. This really helps students to keep independent and dependent variables organized in their minds.                             <ul style="list-style-type: none"> <li>D – dependent</li> <li>R – responsive</li> <li>Y – y-values</li> <li>M – measured</li> <li>I – independent</li> <li>X – x-values</li> </ul> </li> </ul>   |

teaching  
ideas





# ALGEBRAIC REPRESENTATIONS



an 8 day TEKS-aligned unit

TEKS: 6.4A, 6.6A, 6.6B, 6.6C, 6.11A

## unit study guide + assessments



quizzes



editable unit test

Unit: Algebraic Representations  
Quiz 1

Name \_\_\_\_\_  
Date \_\_\_\_\_ Pd \_\_\_\_\_

### QUIZ: ALGEBRAIC REPRESENTATIONS

Answer each of the questions below. Be sure to show your work.

1. Each small moving box,  $m$ , costs \$1.25. Which of the following equations best represents the cost,  $c$ , of buying  $m$  moving boxes?

- A.  $m = 1.25c$       B.  $c = m + 1.25$   
C.  $m = c + 1.25$       D.  $c = 1.25m$

2. Groceries are delivered by a local service. The cost of the groceries is represented by the equation below.

$$c = g + 5.75$$

Which table correctly displays the values?

A.

| G  | C      |
|----|--------|
| 15 | 86.25  |
| 18 | 103.5  |
| 21 | 120.75 |
| 24 | 138    |
| 27 | 155.25 |

B.

| G  | C     |
|----|-------|
| 15 | 20.75 |
| 18 | 23.75 |
| 21 | 26.75 |
| 24 | 29.75 |
| 27 | 32.75 |

3. Which statement best describes the relationship between  $x$  and  $y$  in the equation below?

- A. The value of  $y$  is six less than the value of  $x$ .  
B. The value of  $y$  is six times the value of  $x$ .  
C. The value of  $x$  is six more than the value of  $y$ .  
D. The value of  $y$  is six more than the value of  $x$ .

4. Which statement is **not** true in the equation below?

- A. The value of  $y$  is nine times the value of  $x$ .  
B. The equation represents an additive relationship.  
C. The value of  $y$  is 76.5 when the value of  $x$  is 8.  
D. The equation represents a multiplicative relationship.

Answers

1. \_\_\_\_\_  
2. \_\_\_\_\_  
3. \_\_\_\_\_

Unit: Algebraic Representations  
Review

Name \_\_\_\_\_  
Date \_\_\_\_\_ Pd \_\_\_\_\_

### ALGEBRAIC REPRESENTATIONS UNIT STUDY GUIDE

Solve each of the problems below. These represent the types of questions on your test. Be sure to ask questions if you need more help with a topic.

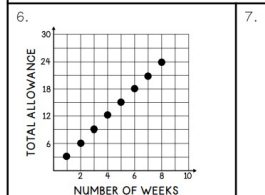
#### I CAN DIFFERENTIATE BETWEEN ADDITIVE & MULTIPLICATIVE RELATIONSHIPS. 6.4A

Label each of the following as an additive or multiplicative relationship.

1.  $y = 7x$   
2.  $y = x - 7$

3. All of Mrs. Palmer's students stood on a 12-inch stool to take class pictures. The height of each student on the stool was represented by  $t$ , while their actual height was represented by  $h$ .

#### I CAN IDENTIFY INDEPENDENT & DEPENDENT QUANTITIES. 6.6A



Independent quantities: \_\_\_\_\_  
Dependent quantities: \_\_\_\_\_

SIXTH GRADE CURRICULUM

# ALGEBRAIC REPRESENTATIONS

UNIT EIGHT: ANSWER KEYS

answer keys  
included



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