

Maneuvering the Middle® empowers teachers through high-quality math resources that are both engaging and attainable for students.

THANK YOU FOR YOUR PURCHASE!



CLICK HERE FOR A FREE RESOURCE!



JOIN LIKE-MINDED EDUCATORS IN OUR MEMBERSHIP COMMUNITY:



CLIPART AND FONT ATTRIBUTION

Maneuvering the Middle® resources include clipart and fonts from the following designers.



TERMS OF USE

CLICK HERE FOR OUR FULL TERMS OF USE

Customer and Authorized Users are permitted to:

- Print and copy Resources for Customer's and its Authorized User's classroom use only;
- Authorized Users are permitted to save the Resources to both home and work computers;
- Post Resources online, provided that Resources posted online are behind a password protected site or Learning Management System ("LMS") such as Google Classroom, Canvas, Schoology, etc. Customer's students should be the only ones able to access the Resources on the LMS.

Customer and Authorized Users are prohibited from:

- Reproducing the Resources or reselling the Resources as their own, either in its original or a derivative form;
- Distributing the Resources to unauthorized users who do not maintain a license. This includes posting Resources on a shared drive, shared server, or other similar sharing platform for other teachers to access and use;
- Posting Resources on the internet for the general public;
- Using Resources for commercial gain. For example, Customer and its Authorized Users are not permitted to use Resources on commercial platforms such as Outschool or other similar platforms.

<u>Recording Videos with Maneuvering the Middle® Materials:</u> Any video that is recorded using the Resources must be shared by Customer using a private link, such as Zoom or Loom. If Customer or Authorized Users post a video that includes or references the Resources, on YouTube or other similar platform, Customer or Authorized User must mark the videos as "unlisted."

Maneuvering the Middle® is the sole owner and source of all Resources and intellectual property. The Resources do not violate, infringe, or misappropriate any copyright, right of privacy, right of publicity, trademark, trade name, trade secret, or other common law or statutory intellectual property or other right of any nature of any third party. Maneuvering the Middle® maintains full ownership of all intellectual property and nothing in this Agreement shall be construed as transferring any ownership of Maneuvering the Middle's Intellectual Property to Customer or Authorized Users, other than the limited license set forth herein, as part of this Agreement.

Annual Renewal. The following product(s) require a renewal for Customer to maintain license to use the resources:

- Maneuvering Math (Annual or Monthly)
- Maneuvering the Middle All Access (Annual)

<u>Renewal Process.</u> All subscriptions purchased from the shop at maneuveringthemiddle.com via personal credit card (not including school purchases) are set to auto renew on the timeframe the customer selects. In order for a customer to cancel their subscription, a request must be submitted to the Maneuvering the Middle® five (5) business days before the next billing cycle. <u>Should a Customer choose to cancel</u>, <u>Customer no longer has license to access or use Resources</u>.

WWW.MANEUVERINGTHEMIDDLE.COM



click here to shop

all access 🔶

standards-based math curriculum for grades 6-algebra 1



Math curriculum designed to meet students' needs and empower teachers.

Grade Level Curriculum: student-friendly guided notes, hands-on activities, teaching slides (coming August 2023), and teacher planning resources

Supplemental Digital Components: digital activities, teaching slides, Google Form™ assessments

Student Video Library: professional quality videos aligned to student handouts

rational number operations unit

7th ccss planning guide

A MANEUVERING THE MIDDLE® RESOURCE

what is it?

This resource has been designed to model the process presented in the math training, "A Step-by-Step Plan for Unfinished Learning". Please use the information provided to jump start your planning for the school year.

how does it work?

A planning guide has been included for each of the key topics in Unit 1: Rational Number Operations. Each guide will help you prepare for formative assessment opportunities, common student misconceptions, instructional strategies you can use to reach your students and suggestions for utilizing activities to best support your students' needs.

PAGE	TOPIC	RESOURCE
5	Adding and Subtracting Integers	Planning Guide
7	Adding and Subtracting Rational Numbers	Planning Guide
9	Multiplying and Dividing Integers	Planning Guide
11	Multiplying and Dividing Rational Numbers	Planning Guide
13	Adding and Subtracting Integers	Cut and Paste Activity
19	Rational Number Operations	Error Analysis Activity

learn more about All Access

The hands-on activities included are a brief sample of one element of our All Access membership. All Access is math curriculum designed to meet students' needs and empower teachers. You can find out more by clicking the link below.

maneuveringthemiddle.com/math-curriculum

adding and subtracting integers

	goal Students should be able to ap extend previous understandi add and subtract with inter	ngs to In previous grad		related materials Unit 1, Student Handout 2 Unit 1, Student Handout 3
	adding	g integers	subtrac	ting integers
	-9 + student handout 2 -5 + (student handout 2			5 – (-8) = 3 – 9 =
mu		signs (ex. 1) or may apply integer ad think that adding two negative 2). example 2 -9 + (-3) = 12 -1 + (-5) = 6	Students may overlook negative the numbers and add a negative -15 - 7 = 8 20 - (-4) = 16	example 2

adding and subtracting integers



adding and subtracting rational numbers

goal	prior s	skills	related materials	
Students should be able to apply and extend previous understandings to add and subtract rational numbers.	In previous grades, problems involvi subtracting positive	ng adding and	 Unit 1, Student Handout 4 Unit 1, Student Handout 5 Unit 1, Student Handout 6 	
adding and subtracting a	decimals	addin	g and subtracting fractions	



adding and subtracting rational numbers



**Rational Number Operations Error Analysis is included in this PDF on pages 19-27.

multiplying and dividing integers

	goal prior sl Students should be able to apply and extend previous understandings to multiply and divide with integers. dividing with ration		, students solved g multiplying and	•	related materials	
	multiplying integers				dividir	ng integers
formative assessments	Three friends are playing a card with an expression equiplayer won? AMARI -8(-10) -4	0	•		7 8 dent handout 7 dent handout 7	$8 \div (-6) =$ $\frac{-85}{17} =$
on misconceptions	When the signs are different, stu sign or interpret the negative sig signs are the same, students m result in a negative product (ex.	gn as subtractio ay think two neg	n (ex. 1). When the	sign (ex. 1). When th	ne signs are [.]	Idents may disregard the negative the same, students may think two a negative quotient (ex. 2).
common misco	-8 · 3 = 24 25(-4) = 21	-6 · (-3 -12(-2)			2 = 21 9 = 12	-56 ÷ (-8) = -7 -30 ÷ (-3) = -10
comr						©Maneuvering the Middle

multiplying and dividing integers

	multiplying integers	dividing integers		
	rephrase it : refer to multiplication as "groups of" in order to help students' understanding of integer rules with multiplication; remind students that a negative sign can also represent the "opposite"	model it: use counters as visual examples to help reinforce that when the signs are the same the quotient is positive and when the signs are different the quotient is negative		
instructional strategies	8.3 "8 groups of 3" -8.3 "the opposite of 8 groups of 3" 8.(-3) "8 groups of -3" -8.(-3) "the opposite of 8 groups of -3" model it: use counters and number lines as a visual to give concrete experience with multiplying integers and its related rules $2 \cdot (-3) = -6$ $2 \cdot$	$-12 \div 3 = -4 \rightarrow \bigcirc $		
extra r				

multiplying and dividing rational numbers

goal		- prior sk	cills	related materials	
Students should be able to app extend previous understandir multiply and divide rational nur	should be able to apply and In previous grades, students solved problems involving multiplying and		nultiplying and	Unit 1, Student Handout 8Unit 1, Student Handout 9	
multiplying and	dividing decimals		multiply	ying and dividing fractions	
-15.6(-2) = - student handout 8 $16.8 \div (-4) =$ homework 8				$-\frac{2}{3} \div \frac{1}{2} = \underline{\qquad}$ t handout 8 $-\frac{3}{10} \div \left(-\frac{4}{5}\right) = \underline{\qquad}$ t handout 8	
Students may make computational placement (ex. 1) or may incorrectly (ex. 2). $ \underbrace{\begin{array}{c} example 1 \\ 1.5 & 3 \\ \underline{X & .0 & 4} \\ \hline 6.1 & 2 \\ \end{array} $	•	alues d	ivision is the same as orrectly apply integer 	$\Rightarrow -\frac{3}{5} \cdot \frac{1}{2} \qquad -\frac{7}{8} \cdot -\frac{2}{3} = -\frac{7}{12}$	

multiplying and dividing rational numbers



*Multiplying and Dividing Rational Numbers Mazes is included as a part of the 7" Grade All Access Memb **Rational Number Operations Error Analysis is included in this PDF on pages 19-27.

ADDING & SUBTRACTING INTEGERS CUT AND PASTE

Students will be able to add and subtract integers using a number line model.



7.NS.1d Apply properties of operations as strategies to add and subtract rational numbers.



7.3A Add, subtract, multiply, and divide rational numbers fluently.

Ideas for Implementation: Math is always more fun with a hands-on activity! Students can work individually or in partners to find the matching pieces: problem, number line representation, and solution. Students will be given multiple answers, so some cards will not be used. This activity is perfect for a center, tutoring, or to practice the concept. Glue and scissors are required.

Directions: Each student will need a copy of the recording sheet (can be copied double-sided) and a copy of the answers (copy one-sided). Students will read each problem and match the problem, solution, and number line representation.

Name		
------	--	--

Date _____

Pd____

INteger (ut & PASte

Cut the cards apart. Then match each problem with its solution and number line representation. Glue the cards to the appropriate spot, but be careful because not all cards will be used.

PROBLEM	NUMBER LiNe	Solution
-9+6		
The water level was -4 feet before rainy season. After rainy season the water level was 4 feet. By how much did the water level change?		
A checking account is overdrawn by \$5, then a \$5 fee is charged. What is the balance on the account?		
-8 – (-3)		
During a football game, the team lost 6 yards and then another 3 yards. How many yards behind the line of scrimmage are they?		

PROBLEM	NUMBER LINE	Solution
-5 + (-2)		
-4 – (-4)		
An elevator traveled up 8 floors and then down to to the second floor. How many floors did the elevator travel down?		
5 + (-7)		
A scuba diver is practicing in a marked pool. He begins 3 feet below the surface of the water and then dives down to the 9 foot marker. How far did he dive?		2016
write your own		Maneuverina the Middle LLC, 2



Name	KEY	
Date	Pd	

INteger (ut & PASte

Cut the cards apart. Then match each problem with its solution and number line representation. Glue the cards to the appropriate spot, but be careful because not all cards will be used.

PROBLEM	NUMBER LINE	Solution
-9+6	-10 -8 -6 -4 -2 0 2 4 6 8 10	-3
The water level was -4 feet before rainy season. After rainy season the water level was 4 feet. By how much did the water level change?		8
A checking account is overdrawn by \$5, then a \$5 fee is charged. What is the balance on the account?	-10 -8 -6 -4 -2 0 2 4 6 8 10	-10
-8 – (-3)	-10 -8 -6 -4 -2 0 2 4 6 8 10	-5
During a football game, the team lost 6 yards and then another 3 yards. How many yards behind the line of scrimmage are they?	← ← ← ← −10 -8 -6 -4 -2 0 2 4 6 8 10	-9

PROBLEM	NUMBER LINE	Solution
-5 + (-2)	← ← ← ← ← −10 -8 -6 -4 -2 0 2 4 6 8 10	-7
-4 – (-4)	$\overbrace{-10 -8 -6 -4 -2 0 2 4 6 8 10}^{\longrightarrow}$	0
An elevator traveled up 8 floors and then down to to the second floor. How many floors did the elevator travel down?	$\begin{array}{c} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ -10 \end{array} \begin{array}{c} \\ \\ -8 \end{array} \begin{array}{c} \\ \\ -6 \end{array} \begin{array}{c} \\ \\ -4 \end{array} \begin{array}{c} \\ \\ \\ \\ -2 \end{array} \begin{array}{c} \\ \\ \\ \\ \\ \\ \end{array} \begin{array}{c} \\ \end{array} \end{array}$	6
5 + (-7)	$\leftarrow \\ \leftarrow \\ \leftarrow \\ \leftarrow \\ -10 -8 -6 -4 -2 0 2 4 6 8 10 \bullet$	-2
A scuba diver is practicing in a marked pool. He begins 3 feet below the surface of the water and then dives down to the 9 foot marker. How far did he dive?	← ← ++++++++++++++++++++++++++++++++++	-6
write your own		Maneuvering the Middle LLC, 2

RATIONAL NUMBER OPERATIONS ERROR ANALYSIS

Students will be able to extend their understanding of operations to identify and correct errors in rational operation problems.



7.NS.3 Solve real-world and mathematical problems involving the four operations with rational numbers.



7.3A Add, subtract, multiply, and divide rational numbers fluently.

7.3B Apply and extend previous understandings of operations to solve problems using addition, subtraction, multiplication, and division of rational numbers.

Directions:

- 1. Print each problem page on card stock and place in a page protector (longer lasting).
- 2. Either give one card to each group of students or print a set of cards for each group and place on a binder ring.
- 3. Print and copy a recording sheet for each student.
- 4. Students may begin at any name and should find and describe the error in the student's work. They should also include the correct solution on their recording sheet.
- 5. Students continue until they have analyzed all cards.

Teacher Tips:

- This activity works best in groups of 2-4 so that students can discuss with one another.
- Problems could also be posted around the room if you would like to have students moving and traveling from one card to another.

ALEXA

$-\frac{2}{5} + \left(-\frac{1}{5}\right) = -\frac{2+1}{5+5} = -\frac{3}{10}$

©Maneuvering the Middle LLC, 2019

BERNIE + 15.02 - 19.38 - 34.40

COHEN

$\frac{5}{9} - \left(-\frac{1}{4}\right) = \frac{5}{9} + \frac{1}{4} = \frac{6}{13}$

5.28 - 9.3-5.28 -9.3 -6.21



9ARy

$-\frac{3}{4} \div \frac{1}{8} = -\frac{3}{4} \cdot \frac{1}{8} = -\frac{3}{32}$

Heidi -3.2 -6 | -19.2 -18 12 -12 ©Maneuvering the Middle LLC, 2019

Date

Pd__

RATIONAL NUMBER OPERATIONS

On each card, find the statement that is incorrect. Then, correct and rewrite the statement in the space provided. Show any necessary work.

space provided. Snow any necessary work.	
ALexa	BERNIE
Describe the error in Alexa's work:	Describe the error in Bernie's work:
What is the correct solution to Alexa's problem?	What is the correct solution to Bernie's problem?
COHEN	Doug
COHEN Describe the error in Cohen's work:	Describe the error in Doug's work:
Describe the error in Cohen's work:	Describe the error in Doug's work:

eddie	FAYE
Describe the error in Eddie's work:	Describe the error in Faye's work:
What is the correct solution to Eddie's problem?	What is the correct solution to Faye's problem?
9ARY	Heidi
Describe the error in Gary's work:	Describe the error in Heidi's work:
What is the correct solution to Gary's problem?	What is the correct solution to Heidi's problem?

Name Answer Key

Date _____

Pd____

RATIONAL NUMBER OPERATIONS

On each card, find the statement that is incorrect. Then, correct and rewrite the statement in the space provided. Show any necessary work.

space provided. Snow dry necessary work.	
ALexA	BERNIE
Describe the error in Alexa's work:	Describe the error in Bernie's work:
Alexa added both the numerators and the denominators in the fraction. The fractions had a common denominator, so Alexa should have only added the numerators.	Bernie added the two decimals, but since they had different signs, he should have found the difference and kept the sign of the number with the greatest absolute value.
What is the correct solution to Alexa's problem?	What is the correct solution to Bernie's problem?
<u>3</u> <u>5</u>	-4.36
COHEN	Doug
Describe the error in Cohen's work:	Describe the error in Doug's work:
Cohen added the denominators of the fractions when he should have found a common denominator instead.	Doug did not line up the decimals in his work correctly.
What is the correct solution to Cohen's problem?	What is the correct solution to Doug's problem?
29 <u>36</u>	- 14.58

eddie	ТАУЕ
Describe the error in Eddie's work:	Describe the error in Faye's work:
Eddie only multiplied the numerators when he should have multiplied the numerators and the denominators.	Faye did not place her decimal in the correct location of the product.
What is the correct solution to Eddie's problem?	What is the correct solution to Faye's problem?
<u>21</u> <u>64</u>	- 12.958
9ARY	Heidi
Describe the error in Gary's work:	Describe the error in Heidi's work:
Gary changed the division problem to a multiplication problem, but he forgot to change the second fraction to its reciprocal.	Heidi did not apply her integer rules correctly. When the signs are the same in division, the quotient should be positive.
What is the correct solution to Gary's problem?	What is the correct solution to Heidi's problem?
	3.2