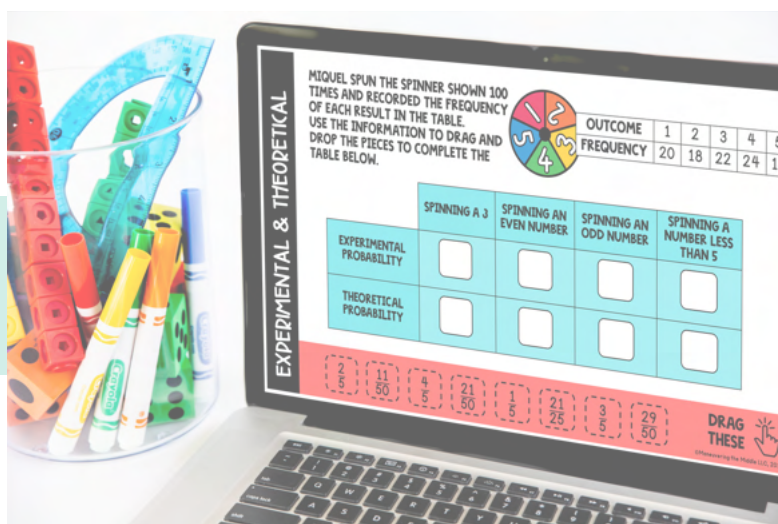# MANEUVERING THE MIDDLE

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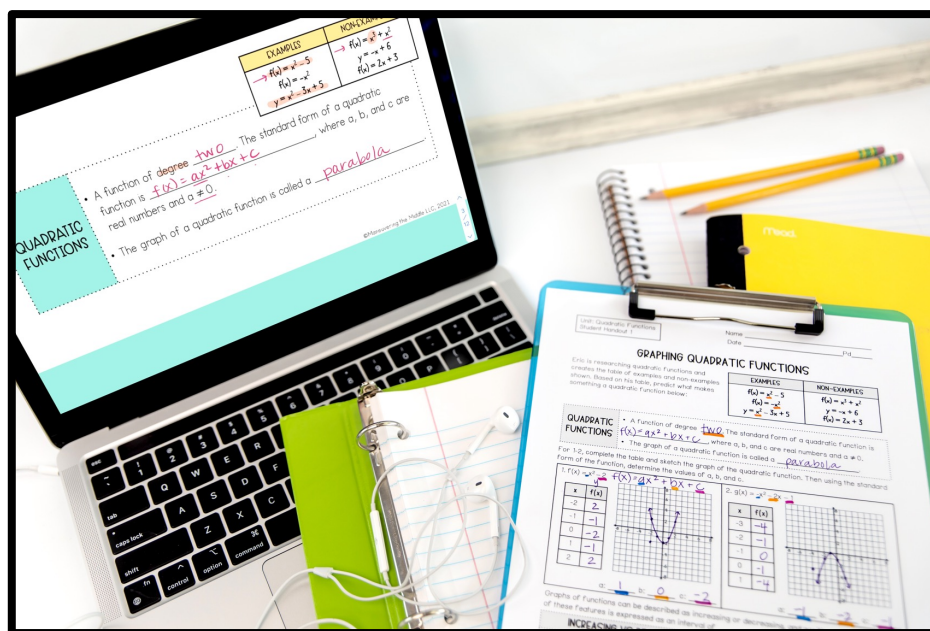
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8th teks planning guide

A MANEUVERING THE MIDDLE® RESOURCE

what is it?

This resource has been designed to model the process presented in the math training, "A Step-by-Step Plan for Unfinished Learning". Please use the information provided to jump start your planning for the school year.

how does it work?

A planning guide has been included for each of the key topics in Unit 1: Real Number System. Each guide will help you prepare for formative assessment opportunities, common student misconceptions, instructional strategies you can use to reach your students and suggestions for utilizing activities to best support your students' needs.

PAGE	TOPIC	RESOURCE
5	Ordering Real Numbers	Planning Guide
7	Classifying Real Numbers	Planning Guide
9	Scientific Notation	Planning Guide
11	Estimating Square Roots	Maze Activity
16	Classifying Real Numbers	Guess My Number Activity

learn more about All Access

The hands-on activities included are a brief sample of one element of our All Access membership. All Access is math curriculum designed to meet students' needs and empower teachers. You can find out more by clicking the link below.

maneuveringthemiddle.com/math-curriculum

ordering real numbers

goal
Students should be able to order a set of real numbers from mathematical and real-world situations.
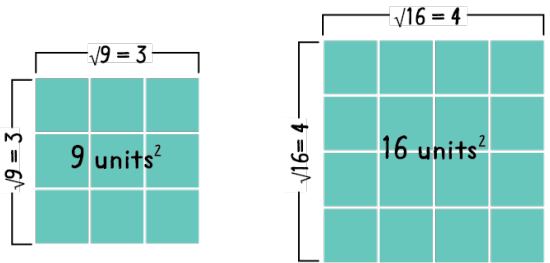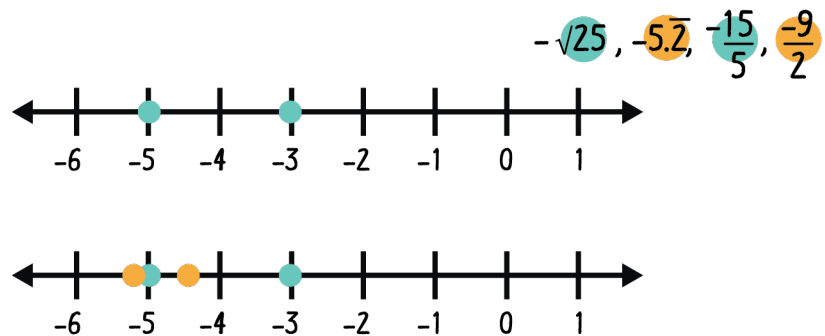
prior skills
In previous grades, students ordered sets of rational numbers.

related materials
- Unit 1, Student Handouts 1-3
- Unit 1, Student Handout 6

	estimating square roots	ordering a set of values
formative assessments	Estimate the value of $\sqrt{50}$. student handout 3 $-\sqrt{12}$ is between _____ and _____. student handout 3	List the following in descending order. $\sqrt{121}$, π^2, 11.1, $\sqrt{130}$ student handout 6 List the following in increasing order. 0.65, 6.5%, $\frac{2}{3}$, $\frac{1}{2}$ student handout 6
common misconceptions	Students may divide by 2 instead of taking the square root (ex. 1) or may struggle to estimate the value of an irrational square root to the nearest tenth (ex. 2). *example 1* $\sqrt{4} = 2$ $\sqrt{16} = 8$ $\sqrt{50} = 25$ *example 2* $\sqrt{27}$ must be between 5 and 6, so about 5.5.	Students may confuse vocabulary such as ascending and descending (ex. 1) or may struggle to order integers correctly (ex. 2). *example 1* $\sqrt{121}$, π^2, 11.1, $\sqrt{130}$ *If ordering the list above in descending order, a student may list the values from least to greatest instead of greatest to least.* *example 2* $-\sqrt{144}$, $-\frac{13}{2}$, -8.5, -3^2 *If ordering the list above from least to greatest, a student might start with $-\frac{13}{2}$, the "smallest" negative rather than $-\sqrt{144}$, the value that is the furthest from zero.*

ordering real numbers

	estimating square roots	ordering a set of values
instructional strategies	**model it:** have students cut out squares of various dimensions from graph paper to observe the relationship between the area of a square and the side length of the square; this is also a good way to reinforce the concept of "perfect squares" **model it:** encourage students to sketch a number line to organize their thinking and identify two integers that a non-perfect square must lie between	**model it:** encourage students to always sketch a number line to organize their thinking and avoid errors, especially when ordering integers **organize it:** when given a list of values to order, have students first place the whole numbers and integers on the number line (including fractions and/or square roots that simplify to integers) and then place the fractions, decimals and/or non-perfect square roots $$-\sqrt{25},\ -5.\overline{2},\ \frac{-15}{5},\ \frac{-9}{2}$$
extra practice and resources	**Estimating Square Roots Mazes*** Consider using the maze that best needs the meets of your students according to the types of values included on each maze: • Maze #1: Square roots of numbers ≤ 100 • Maze #2: Square roots of numbers ≤ 225	For extra practice, give groups of students index cards with a value written on each and ask the group to order their cards in ascending or descending order. Be sure to include different forms such as fractions, decimals, percentages, and square roots. Students could also use masking tape to create a number line and order the cards on the line.

*Estimating Square Roots Mazes is included in this PDF on pages 11-15.

classifying real numbers

goal

Students should be able to describe relationships between sets of real numbers.

prior skills

In previous grades, students classified rational numbers.

related materials

- Unit 1, Student Handouts 1-2
- Unit 1, Student Handouts 4-5

distinguishing rational vs irrational numbers	representing relationships between real numbers

formative assessments

Classify each given value as rational or irrational. Explain your choice in the last column.

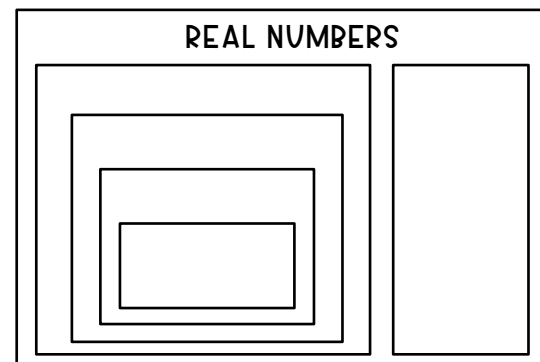| VALUE	RATIONAL OR IRRATIONAL?	EXPLANATION
-12		
π		

student handout 4

Place the headings for each type of real number in the graphic organizer below. Then, write the following values in the box where they belong.

VALUES:

$2\sqrt{64}$ -15 $\dfrac{16}{4}$

$\sqrt{75}$ 0 -12.2

REAL NUMBERS

student handout 5

common misconceptions

Students may classify all square roots as irrational (ex. 1) or may forget to simplify a value before classifying (ex. 2).

example 1

$\sqrt{64}$ is an irrational value because it is represented as a square root.

example 2

The most specific set $-\dfrac{36}{12}$ belongs to is rational since it is expressed as a ratio.

Students may think that numbers only belong to one set (ex. 1) or misapply logic related to sets and subsets (ex. 2).

example 1

$-\dfrac{15}{3} \rightarrow$ integer

example 2

If all rational numbers are real numbers, then all real numbers must be rational numbers.

classifying real numbers

	distinguishing rational vs irrational numbers	representing relationships between real numbers
instructional strategies	**rephrase it:** give students an opportunity to complete the following sentences in their own words: • Rational values include _____ • Irrational values include _____ **model it:** allow students to input a non-perfect square root on their calculator to see how an irrational value is displayed	**model it:** allow students to practice organizing relationships between a category they are familiar with before applying the practice to real numbers in order to solidify concepts of sets and subsets (ex. a graphic organizer that organizes the people at your school) Consider asking, "Is it possible to be included in the section for 8th graders but not in the section for students? What about the other way around?"
extra practice and resources	**Rational vs Irrational Numbers Card Sort*** The cards include values represented as fractions, decimals and square roots. Consider having students verbally complete the sentences below when sorting a card based on the representation: • This **fraction** is classified as _____ because _____ • This **decimal** is classified as _____ because _____ • This **square root** is classified as _____ because _____	**Classifying Real Numbers Guess My Number**** Utilize this activity in groups to reinforce the definitions and distinguishing characteristics of different types of real numbers. Consider the following ideas during the activity: • Allow students to use a graphic organizer as they read each statement to show their thinking and provide a visual understanding of the clues • Consider extending the activity by asking students to create their own clues to describe a mystery number

*Rational vs Irrational Numbers Card Sort is included as a part of the 8th Grade All Access Membership.
**Classifying Real Numbers Guess My Number is included in this PDF on pages 16-23.

scientific notation

converting from standard to scientific notation	converting from scientific to standard notation
formative assessments — Convert each given value to scientific notation. 1,850,000 student handout 7 0.007826 student handout 7	Convert each given value to standard form. 7.83×10^7 student handout 7 8.345×10^{-6} student handout 7
common misconceptions — Students may forget to include the negative sign with the exponent when expressing very small values in scientific notation (ex. 1) or may incorrectly place the decimal (ex. 2).	Students may move the decimal the wrong direction (ex. 1) or may automatically add the same number of zeroes to the value in standard notation as the exponent (ex. 2).

common misconceptions

converting from standard to scientific notation:

example 1	example 2
0.000000029	12,000,000
2.9×10^8	12×10^6

converting from scientific to standard notation:

example 1	example 2
3.4×10^{-4}	5.23×10^7
34,000	5,230,000,000

scientific notation

	converting from standard to scientific notation	converting from scientific to standard notation
instructional strategies	**rephrase it:** to help students determine whether a positive or negative exponent is reasonable, ask if the standard notation represents a large or small number (students should start to generalize that large numbers will require a positive exponent and decimals less than one will require a negative exponent) $9500.0 = 9.5 \times 10^{3}$ $9500 = 9.5 \times 10^{3}$ $0.0095 = 9.5 \times 10^{-3}$ $0.0095 = 9.5 \times 10^{-3}$	**model it:** in order to make sense of "moving the decimal" the same number of places as the exponent, show a string of multiplication problems where students multiply a decimal value by 10, 100 and 1,000. Then, show the exponent notation of 10 (10^1), 100 (10^2) and 1,000 (10^3) to make the connection that the decimal moved the same number of places as the exponent. $8.23 \times 10 = 82.3$ $8.23 \times 10^{1} = 82.3$ $8.23 \times 100 = 823.0$ $8.23 \times 10^{2} = 823.0$ $8.23 \times 1000 = 8230.0$ $8.23 \times 10^{3} = 8230.0$
extra practice and resources	Scientific Notation Scavenger Hunt* Consider using the scavenger hunt in two different ways. First, as a traditional scavenger hunt to promote movement and collaboration. Second, use the scavenger hunt as a set of cards that can be scaffolded in a small group setting. The skills practiced on each card are listed below. Cards 1, 2, 6 and 7 could be practiced in a small group before allowing students to continue with the rest. • Cards 1-5 practice converting from standard notation to scientific notation • Cards 6-10 practice converting from scientific notation to standard notation	

*Scientific Notation Scavenger Hunt is included as a part of the 8th Grade All Access Membership.

ESTIMATING SQUARE ROOTS
MAZE ACTIVITY

Students will be able to approximate and locate irrational numbers on a number line.

CCSS

8.NS.2 Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., π^2).

TEKS

8.2B Approximate the value of an irrational number, including π and square roots of numbers less than 225, and locate that rational number approximation on a number line

Ideas for Implementation: This activity challenges student ability to estimate non-perfect square roots. There are two different mazes included. Maze #1 includes square roots of numbers less than or equal to 100 and Maze #2 includes square roots of numbers less than or equal to 225.

Instructions:
1) Print and copy a maze (or both mazes) for each student.

2) Students will pick the expression that results in the best estimate of the point plotted on each number line. Accurate selections will lead them correctly to the finish.
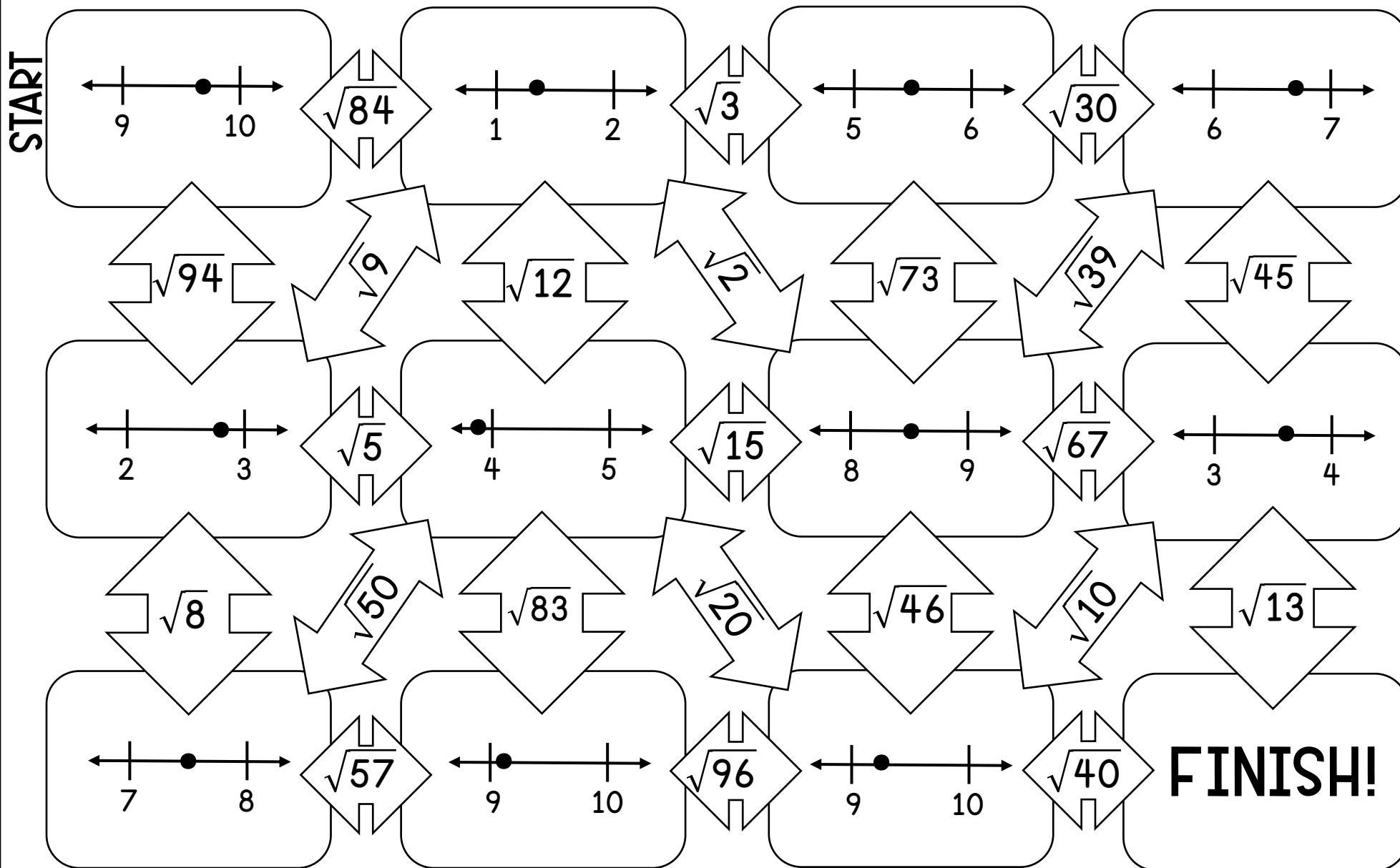
Notes: Consider having students shade the path with a highlighter or colored pencils for easy grading. This activity is best used as an individual assessment and is great for early finishers.

ESTIMATING SQUARE ROOTS

Name: _____ Date: _____ Pd: _____

MAZE #1

Instructions: Follow the best estimate of each square root plotted on the number lines to make it correctly through the maze. Shade or color your path as you go.
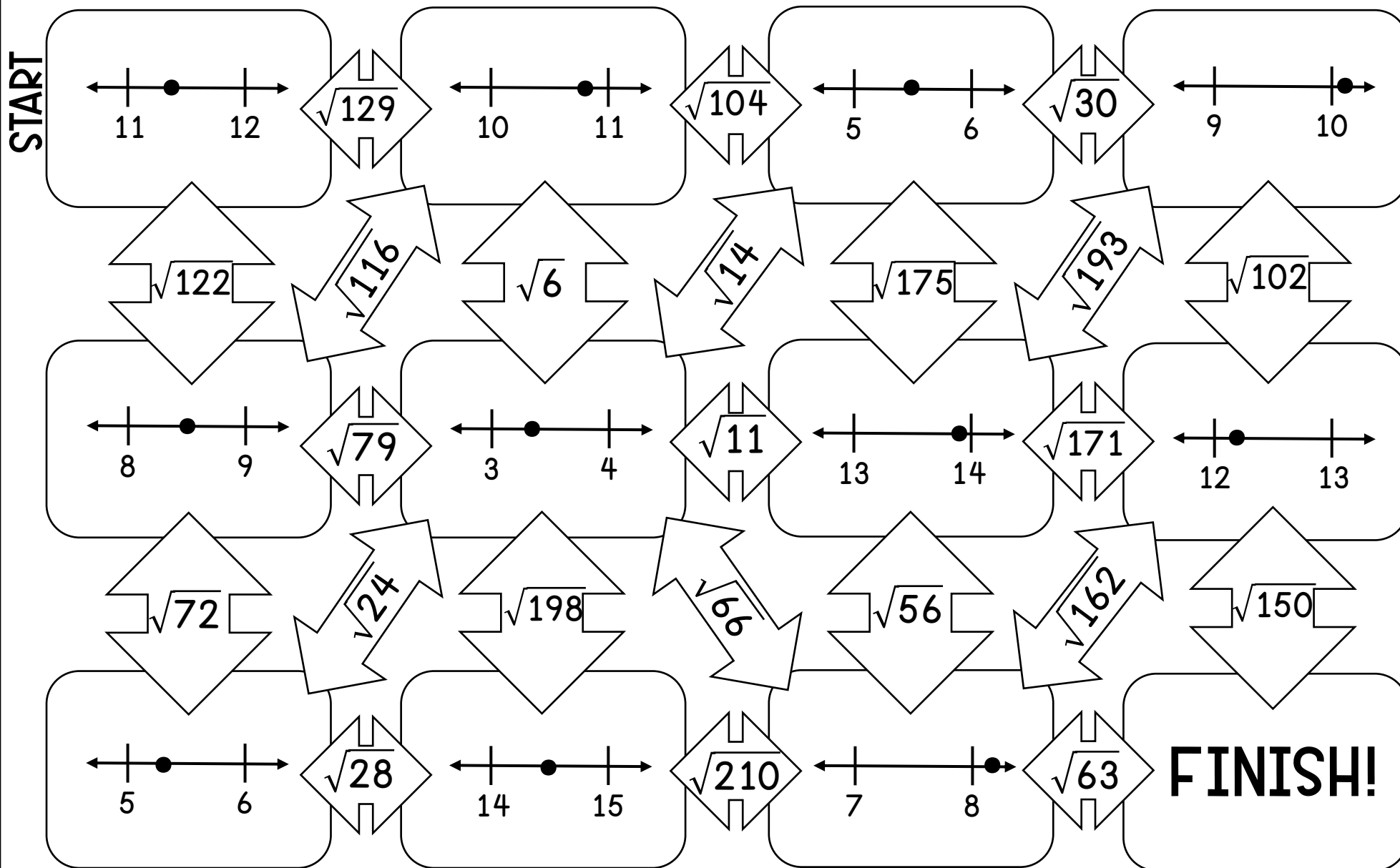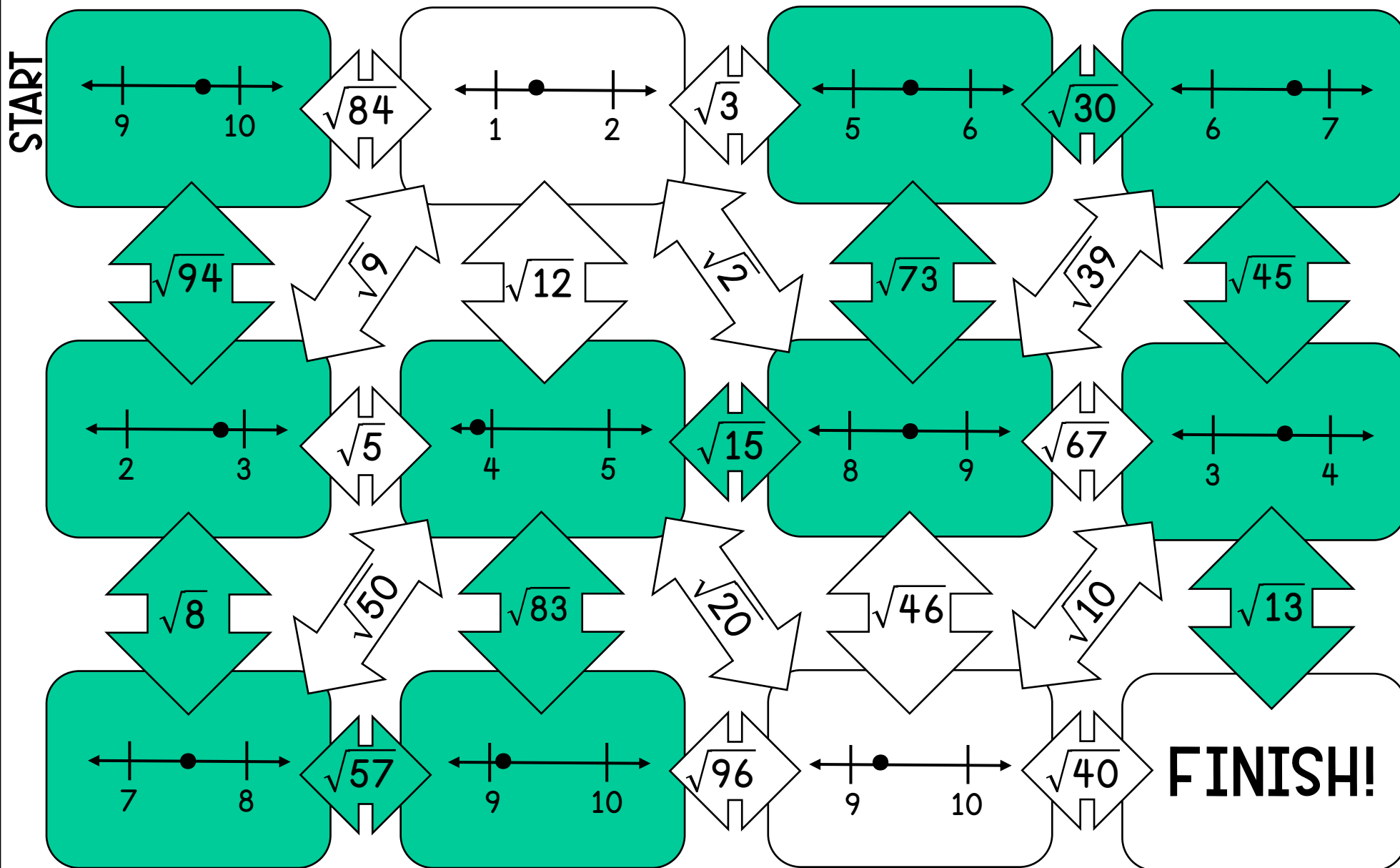
START

$\sqrt{84}$ $\sqrt{3}$ $\sqrt{30}$

$\sqrt{94}$ $\sqrt{9}$ $\sqrt{12}$ $\sqrt{2}$ $\sqrt{73}$ $\sqrt{39}$ $\sqrt{45}$

$\sqrt{5}$ $\sqrt{15}$ $\sqrt{67}$

$\sqrt{8}$ $\sqrt{50}$ $\sqrt{83}$ $\sqrt{20}$ $\sqrt{46}$ $\sqrt{10}$ $\sqrt{13}$

$\sqrt{57}$ $\sqrt{96}$ $\sqrt{40}$

FINISH!

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ESTIMATING SQUARE ROOTS

Name: _____ Date: _____ Pd: _____

MAZE #2

Instructions: Follow the best estimate of each square root plotted on the number lines to make it correctly through the maze. Shade or color your path as you go.
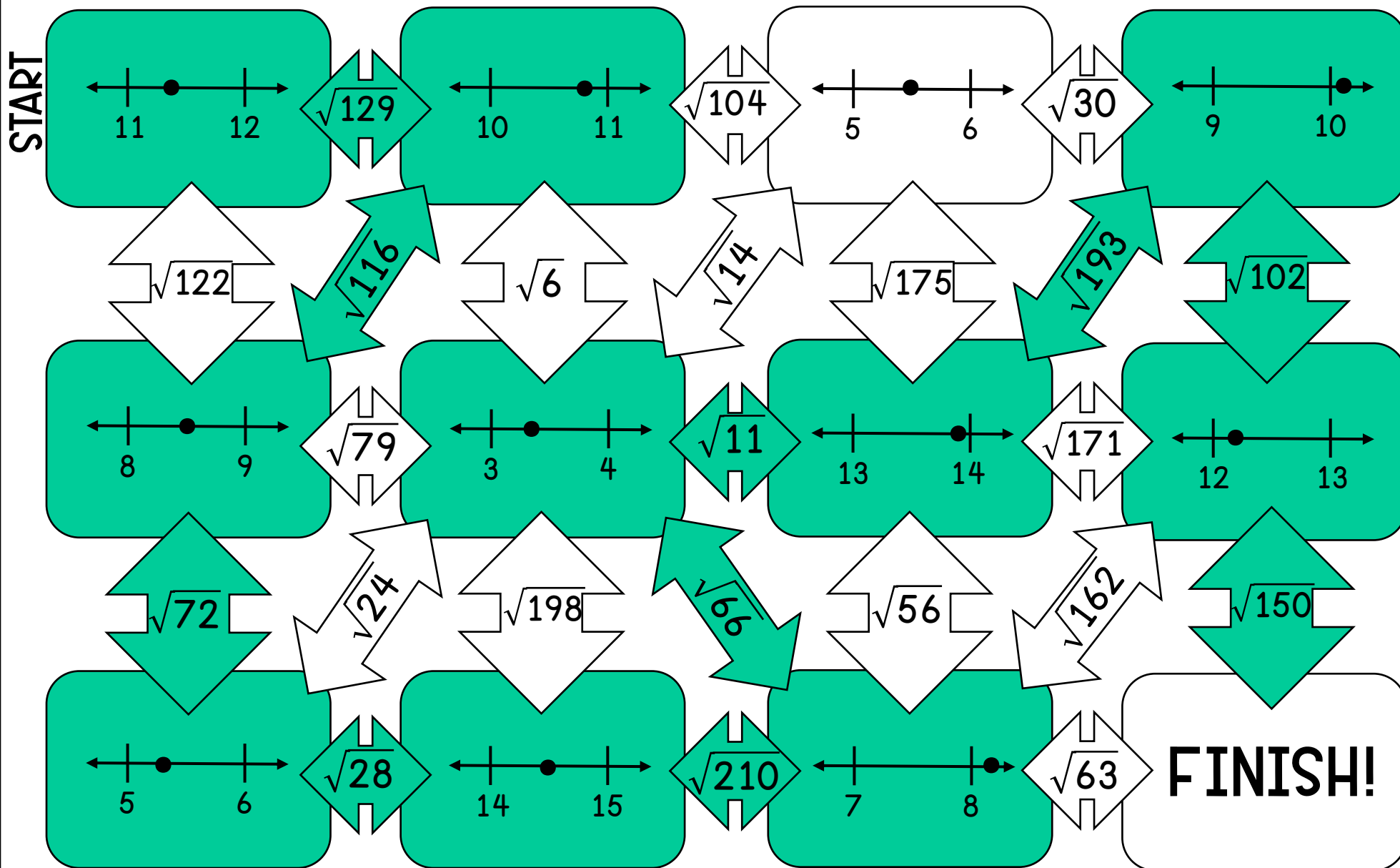
START

Number line (11 to 12, dot near 11) — $\sqrt{129}$

Number line (10 to 11, dot near 11) — $\sqrt{104}$

Number line (5 to 6, dot near middle) — $\sqrt{30}$

Number line (9 to 10, dot near 10)

$\sqrt{122}$ — $\sqrt{116}$ — $\sqrt{6}$ — $\sqrt{14}$ — $\sqrt{175}$ — $\sqrt{193}$ — $\sqrt{102}$

Number line (8 to 9, dot near middle) — $\sqrt{79}$

Number line (3 to 4, dot near middle) — $\sqrt{11}$

Number line (13 to 14, dot near 14) — $\sqrt{171}$

Number line (12 to 13, dot near 12)

$\sqrt{72}$ — $\sqrt{24}$ — $\sqrt{198}$ — $\sqrt{66}$ — $\sqrt{56}$ — $\sqrt{162}$ — $\sqrt{150}$

Number line (5 to 6, dot near middle) — $\sqrt{28}$

Number line (14 to 15, dot near middle) — $\sqrt{210}$

Number line (7 to 8, dot near 8) — $\sqrt{63}$

FINISH!

ESTIMATING SQUARE ROOTS

Name: _____KEY_____ Date: _____ Pd: _____

MAZE #1

Instructions: Follow the best estimate of each square root plotted on the number lines to make it correctly through the maze. Shade or color your path as you go.

START

$\sqrt{84}$ $\sqrt{3}$ $\sqrt{30}$

$\sqrt{94}$ $\sqrt{9}$ $\sqrt{12}$ $\sqrt{2}$ $\sqrt{73}$ $\sqrt{39}$ $\sqrt{45}$

$\sqrt{5}$ $\sqrt{15}$ $\sqrt{67}$

$\sqrt{8}$ $\sqrt{50}$ $\sqrt{83}$ $\sqrt{20}$ $\sqrt{46}$ $\sqrt{10}$ $\sqrt{13}$

$\sqrt{57}$ $\sqrt{96}$ $\sqrt{40}$

FINISH!

ESTIMATING SQUARE ROOTS

Name: __KEY__ Date: _____ Pd: _____

MAZE #2

Instructions: Follow the best estimate of each square root plotted on the number lines to make it correctly through the maze. Shade or color your path as you go.

START

$\sqrt{129}$ · 11 12

$\sqrt{104}$ · 10 11

$\sqrt{30}$ · 5 6

· 9 10

$\sqrt{122}$ $\sqrt{116}$ $\sqrt{6}$ $\sqrt{14}$ $\sqrt{175}$ $\sqrt{193}$ $\sqrt{102}$

· 8 9 $\sqrt{79}$ · 3 4 $\sqrt{11}$ · 13 14 $\sqrt{171}$ · 12 13

$\sqrt{72}$ $\sqrt{24}$ $\sqrt{198}$ $\sqrt{66}$ $\sqrt{56}$ $\sqrt{162}$ $\sqrt{150}$

· 5 6 $\sqrt{28}$ · 14 15 $\sqrt{210}$ · 7 8 $\sqrt{63}$ **FINISH!**

CLASSIFYING REAL NUMBERS
"Guess My Number"

Students will be able to classify types of real numbers.

CCSS

8.NS.1 Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which repeats eventually into a rational number.

TEKS

8.2.A Extend previous knowledge of sets and subsets using a visual representation to describe relationships between sets of real numbers.

Ideas for Implementation: This activity reinforces student's knowledge of real numbers and sets of real numbers as students use clues to correctly identify a number being described.

Instructions:

1) Print and copy a recording sheet for each student.

2) Print and copy the clue cards onto cardstock and cut into half sheets.

3) Students can start at any clue card and will read the clues to correctly match all 10 numbers to their clues.

Notes: You could make one set of the clues and post them around the room for students to walk to in small groups. Otherwise, cards could be placed on a binder ring in order to give individual sets of clue cards to smaller groups.

Name _____

Date _____ Pd_____

GUESS MY NUMBER: RECORDING SHEET

INSTRUCTIONS: The 10 cards with clues describe the 10 numbers in the table below. Use the clues given on the 10 cards and your knowledge of real numbers in order to help you correctly match each number. Record your guesses by each magnifying glass.

-10	$\sqrt{70}$	3	$\sqrt{120}$	0
$-12\frac{2}{3}$	1.8	$-\sqrt{225}$	$\frac{4}{3}$	π

#1 _____	#6 _____
#2 _____	#7 _____
#3 _____	#8 _____
#4 _____	#9 _____
#5 _____	#10 _____

- I AM NOT IRRATIONAL

- I AM AN INTEGER

- I AM A NATURAL NUMBER

- I AM A PRIME NUMBER

- WHAT NUMBER AM I?

#1

- I AM IN A SUBSET OF RATIONAL NUMBERS

- I AM NOT NEGATIVE

- I AM A WHOLE NUMBER

- I AM NOT A NATURAL NUMBER

- WHAT NUMBER AM I?

#2

- I AM NOT IRRATIONAL

- MY OPPOSITE IS A NATURAL NUMBER

- I AM NOT A WHOLE NUMBER

- I AM GREATER THAN -13

- WHAT NUMBER AM I?

#3

- I AM A REAL NUMBER

- I AM A RATIONAL NUMBER

- I AM NOT A NATURAL NUMBER

- I AM LESS THAN -13

- WHAT NUMBER AM I?

#4

- I AM NOT IRRATIONAL

- I AM NOT A WHOLE NUMBER

- I AM NOT AN INTEGER

- I AM NOT POSITIVE

- WHAT NUMBER AM I?

#5

- I AM A REAL NUMBER

- I AM NON-TERMINATING AS A DECIMAL

- I AM NOT A WHOLE NUMBER

- I AM BETWEEN 8 & 9

- WHAT NUMBER AM I?

#6

- I AM NOT AN INTEGER

- I AM NOT A REPEATING DECIMAL

- I AM IMPOSSIBLE TO WRITE AS A FRACTION

- I AM BETWEEN 3 & 4

- WHAT NUMBER AM I?

#7

- I CAN BE WRITTEN AS A FRACTION

- I AM NOT A NATURAL NUMBER

- I AM NOT AN INTEGER

- I AM A TERMINATING DECIMAL

- WHAT NUMBER AM I?

#8

- I CAN BE WRITTEN AS A RATIO

- I AM NOT A NEGATIVE NUMBER

- I AM NOT A WHOLE NUMBER

- I WOULD BE REPEATING AS A DECIMAL

- WHAT NUMBER AM I?

#9

- I AM NOT A NATURAL NUMBER

- I AM NOT A TERMINATING DECIMAL

- I CAN'T BE WRITTEN AS A RATIO

- I AM GREATER THAN 10 BUT LESS THAN 11

- WHAT NUMBER AM I?

#10

GUESS MY NUMBER: RECORDING SHEET

INSTRUCTIONS: The 10 cards with clues describe the 10 numbers in the table below. Use the clues given on the 10 cards and your knowledge of real numbers in order to help you correctly match each number. Record your guesses by each magnifying glass.

-10	$\sqrt{70}$	3	$\sqrt{120}$	0
$-12\frac{2}{3}$	1.8	$-\sqrt{225}$	$\frac{4}{3}$	π

#1	3	#6	$\sqrt{70}$
#2	0	**#7**	π
#3	-10	**#8**	1.8
#4	$-\sqrt{225}$	**#9**	$\frac{4}{3}$
#5	$-12\frac{2}{3}$	**#10**	$\sqrt{120}$